



**LEBANESE AMERICAN UNIVERSITY**

School of Engineering

Department of Electrical and Computer Engineering

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ELE443 Control System LAB

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## Lecture 1: Introduction to MATLAB

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# Introduction

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- ▶ **MATLAB=Matrix Laboratory**
- ▶ MATLAB is a high-performance language for technical computing.
- ▶ It integrates computation, visualization, and programming in an easy-to-use environment.
  
- ▶ Typical uses are:
  - ▶ Math and computation
  - ▶ Algorithm development
  - ▶ Data acquisition
  - ▶ Modeling
  - ▶ simulation, and prototyping
  - ▶ Data analysis, exploration, and visualization
  - ▶ Scientific and engineering graphics
  - ▶ Application development, including graphical user interface building

# MATLAB System

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- ▶ MATLAB System is formed of 5 main parts:
  - ▶ Desktop Tools and Development Environment
  - ▶ The MATLAB Mathematical Function Library
  - ▶ The MATLAB Language
  - ▶ Graphics
  - ▶ The MATLAB External Interfaces/API

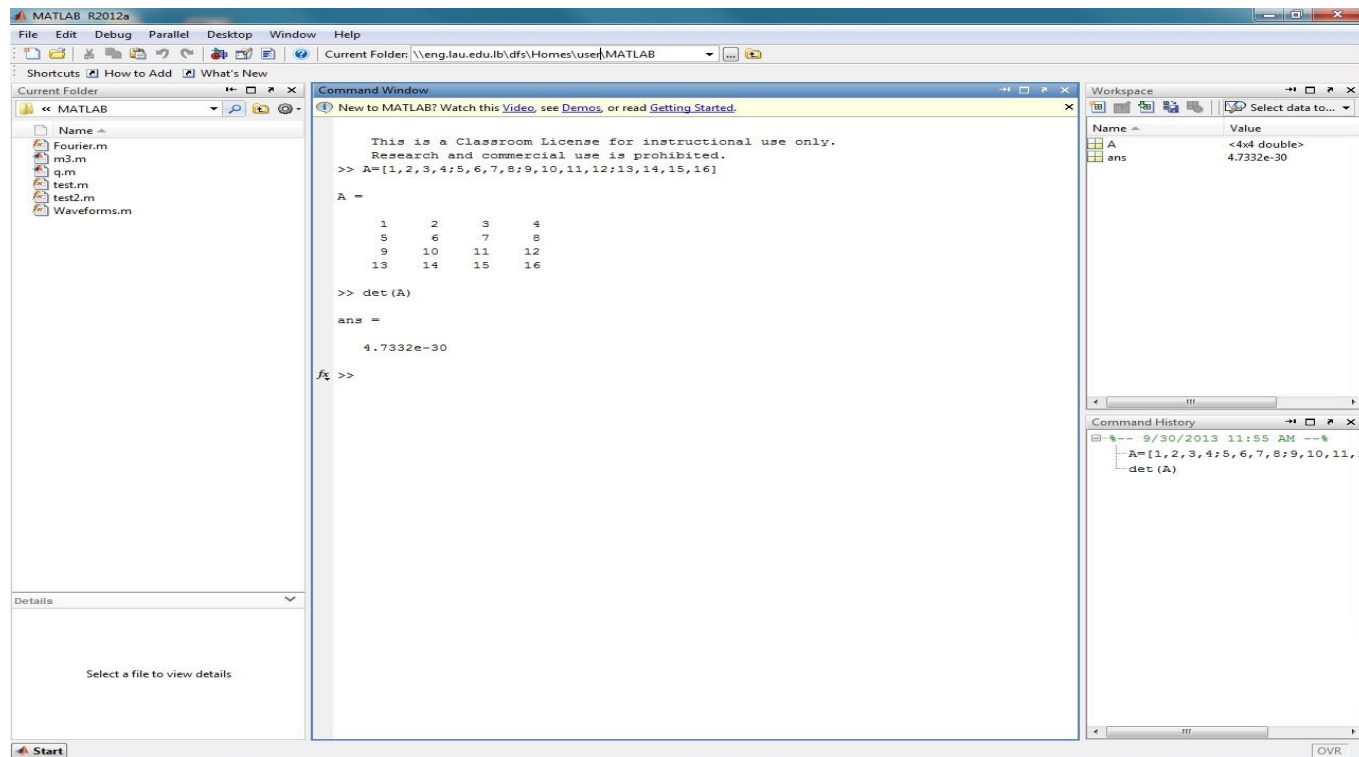
# MATLAB Toolboxes

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- ▶ There are many toolboxes in MATLAB:
  - ▶ Control Systems Toolbox
  - ▶ Communication Toolbox
  - ▶ Curve Fitting Toolbox
  - ▶ Filter Design Toolbox
  - ▶ Statistics Toolbox
  - ▶ ...
- ▶ In addition to Simulink which simulates systems using block diagrams

# MATLAB Windows

- ▶ Command Window
- ▶ Current Directory
- ▶ Workspace
- ▶ Command History



# Basic Notations

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- ▶ **Semicolon(;):** If a semicolon is typed after a command, then the command is executed without displaying the output.
- ▶ **Comments(%):** Similarly to high level programming languages, comments in MATLAB codes are written after typing percent sign %
- ▶ **clear:** It clears all variables in workspace
- ▶ **clear A B:** Clears variables A and B from workspace
- ▶ **clc:** Clears the command window and homes the cursor. It doesn't affect workspace variables
- ▶ **close:** Closes the current figure window
- ▶ **help plot:** Gives information about the use and the arguments of a function. In this case, it gives information about the function "plot"
- ▶ **exit:** Exit MATLAB

# Arithmetic Operators

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Symbol	Operation
+	Addition
-	Subtraction
*	Multiplication
/	Division
\	Left division
^	Power
'	Complex conjugate transpose
()	Specify evaluation order

# Arithmetic Operations

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- ▶ MATLAB as a **calculator**:
  - ▶ Simplest way to use MATLAB
    - ▶ Type command (mathematical expression)
    - ▶ Press Enter Key
    - ▶ Command executed and then is displayed
      - ans= (result)
  - ▶ Example
    - ▶ `cos(pi/2)`  
ans = 0



# Display Format

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- ▶ The number format in command window can be modified using the command **format**
- ▶ The default format in the command window is the **short** representation of numbers.

Command	Description	Example
format short	Scaled fixed point format, with 5 digits	3.1416
format long	Scaled fixed point format, with 15 digits for double; 7 digits for single.	3.14159265358979

# Display Format

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Command	Description	Example
format short eng	Engineering format that has at least 5 digits and a power that is a multiple of three	3.1416e+000
format long eng	Engineering format that has exactly 16 significant digits and a power that is a multiple of three	3.14159265358979e+000
format short e	Floating point format, with 5 digits.	3.1416e+000
format long e	Floating point format, with 15 digits for double; 7 digits for single.	3.141592653589793e+000

# Elementary functions

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- ▶ MATLAB has built-in useful elementary functions, and extended lists of elementary functions is provided by MATLAB toolboxes.
- ▶ Some useful elementary functions:
  - ▶ `sqrt`, `exp`, `log`, `log10`, `log2`, `cos`, `ceil`, `sign`

# MATLAB Variables

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- ▶ The MATLAB language works with only a single object type: the **MATLAB array**.
- ▶ All MATLAB variables, including scalars, vectors, matrices, strings, cell arrays, structures, and objects are stored as MATLAB arrays.
- ▶ Variables are shown in **Workspace**.
- ▶ Variables can have different data types such as:
  - ▶ Complex Double-Precision Matrices
  - ▶ Numeric Matrices
  - ▶ Logical Matrices
  - ▶ MATLAB Strings
  - ▶ Empty Arrays

# MATLAB Variables

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## ▶ Variable

- ▶ Name made of a combination of letters and/or digits:
  - ▶ Memory location
- ▶ Scalar variables are assigned a numerical value:
  - ▶ Stored in memory location
- ▶ Can be used in any MATLAB statement or command

▶ Variables are assigned using equal operator (=). It assigns a value to a variable

## ▶ Example:

$x = \pi/2$                        $f = \sin(x)$

$x = 1.5708$                        $f = 1$

# MATLAB Variables

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## ▶ Rules about variable names:

- ▶ Up to 63 characters in MATLAB 7 (31 in MATLAB 6.x).
- ▶ Can contain letters, digits and underscore.
- ▶ Must begin with a letter.
- ▶ MATLAB is case sensitive.
- ▶ Avoid using names of built-in functions or predefined variables.

## ▶ Predefined variables

- ▶ `pi` = the number  $\pi$
- ▶ `Inf` =Infinity
- ▶ `realmax`=Largest positive floating point number
- ▶ `realmin`=Smallest positive floating point number
- ▶ `i` = `sqrt(-1)`
- ▶ `j` = `I`
- ▶ `NaN`= (Not a Number) used by MATLAB when it cannot define a valid numerical value, such as `0/0`.
- ▶ `Eps` = Spacing of floating point numbers =  $2^{-52}$

# MATLAB Variables

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## ► Useful commands for managing variables

<b>Command</b>	<b>Description</b>
<code>clear</code>	Clear variables and functions from memory.
<code>clear x y</code>	Clear the variables specified.
<code>who</code>	List current variables.
<code>whos</code>	List current variables, long form.
<code>load</code>	Load workspace variables from disk.
<code>save</code>	Save workspace variables to disk.

# Creating Arrays in MATLAB

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## ▶ Array:

- ▶ Fundamental form used to store and manipulate data.
- ▶ Arranged in rows and/or columns.
- ▶ Include data of different types.
- ▶ Arrays are n-dimensional:
  - ▶ One-Dimensional (Vector)
  - ▶ Two-Dimensional (Matrix)
  - ▶ N-Dimensional



# Arrays

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- ▶ **Array constructor [ ]**
  - ▶ An array of elements (Vector or Matrix) is created using brackets [ ]
- ▶ **Example:**
  - ▶  $V=[1\ 2\ 3\ 5]$  creates a horizontal vector
  - ▶ Similarly,  $V=[1,2,3,5]$
- ▶ A **Comma** or a **Blank** separate between elements in two columns of a matrix or vector

# Creating Vectors

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- ▶ When vector elements are specified element by element, a vector can be defined as follows:

- ▶ **Row vector:**

- ▶  $V=[1\ 2\ 3\ 5]$

- $V = 1\quad 2\quad 3\quad 5$

- ▶ **Column Vector:**

- ▶ Elements in a column vector are separated using semicolon(;)

- ▶  $U=[5;2;1]$

- $U = 5$

- $2$

- $1$

# Creating Vectors

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- ▶ Vectors with constant spacing:
  - ▶  $V = \text{start} : \text{space} : \text{end}$
  - ▶ start= first element, end=last element
  - ▶ space= spacing between two consecutive elements
  
- ▶  $V = 1 : 3 : 13$   
 $V = 1 \quad 4 \quad 7 \quad 10 \quad 13$
  
- ▶ When **space** is omitted, default spacing is 1.

# Creating Vectors

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- ▶ Vector with constant spacing of a desired number of elements:
- ▶ **`V=linspace(start,end,# of elements)`**
  - ▶ `V=linspace(1,5,3)`  
`V = 1    3    5`
- ▶ When # of elements is omitted, 100 is used as a default number.

# Creating Matrices

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- ▶ Matrices are two-dimensional arrays.
  - ▶ An **m-by-n** matrix has **m** rows and **n** columns
  - ▶ All rows must have the same number of elements.
  - ▶ In square matrices,  $m=n$ .

- ▶ Example:

$$A=[1 \ 5 \ 7;8 \ 2 \ 6;4 \ -2 \ 9]$$

$$A = \begin{matrix} 1 & 5 & 7 \\ 8 & 2 & 6 \\ 4 & -2 & 9 \end{matrix}$$

# Creating Matrices

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- ▶ Variables or functions with adequate output size can be used to define matrix elements.

- ▶  $x=0;$   
 $y=\pi/6;$   
 $z=\pi/2;$

- ▶  $A=[x,y,z]$

$$A = 0 \quad 0.5236 \quad 1.5708$$

- ▶  $B=[A;\sin(A)]$

$$B = \begin{matrix} 0 & 0.5236 & 1.5708 \\ 0 & 0.5 & 1 \end{matrix}$$

# Useful matrices

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- ▶ `zeros(M,N)`

- ▶ Creates an M-by-N matrix of zeros.

- ▶ `ones(M,N)`

- ▶ Creates an M-by-N matrix of ones.

- ▶ `eye(N)`

- ▶ Creates the N-by-N identity matrix.

# 3-Dimensional Arrays

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- ▶ A 3D array may be constructed by *superposition* of 2D arrays.

- ▶ Example:

- ▶  $A = [1 \ 2 \ 5; 7 \ 8 \ 6];$

- ▶  $B = [8 \ 2 \ 6; 7 \ 3 \ 1];$

- ▶  $C(:,:,1) = A$

$$C = \begin{matrix} 1 & 2 & 5 \\ 7 & 8 & 6 \end{matrix}$$

- ▶  $C(:,:,2) = B$

$$C(:,:,1) = \begin{matrix} 1 & 2 & 5 \\ 7 & 8 & 6 \end{matrix}$$
$$C(:,:,2) = \begin{matrix} 8 & 2 & 6 \\ 7 & 3 & 1 \end{matrix}$$



# The Transpose Operation

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- ▶ In vectors: Switches row (column) to column (row)
- ▶ In matrices: Switches columns (rows) to rows (columns)
- ▶ Applied by typing ' next to a variable.
- ▶ Transpose is not defined for N-Dimensional arrays where  $N > 2$

- ▶ Example:

```
A = [1 2 5; 7 8 6]
```

```
A = 1    2    5
```

```
     7    8    6
```

```
>> A'
```

```
ans = 1    7
```

```
      2    8
```

```
      5    6
```

# Array Addressing

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- ▶ Elements in arrays can be addressed individually or in subgroups.
- ▶ In vectors, elements are addressed by their index.
- ▶ Vector indices start from 1.

▶ For example:

▶  $V=[5\ 4\ 8\ 3\ 7];$

$V(1)$   
 $\text{ans} = 5$

$a=V(5)$   
 $a = 7$

# Array Addressing

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- ▶ Elements of N-Dimensional arrays are addressed using N coordinates (arguments).
- ▶ Matrices are 2D arrays.

- ▶  $A = [5 \ 6 \ 3; 8 \ 2 \ -9]$   
 $A = \begin{matrix} 5 & 6 & 3 \\ 8 & 2 & -9 \end{matrix}$

- ▶ The element “-9” is in the 2<sup>nd</sup> row and 3<sup>rd</sup> column can be addressed by:
  - ▶  $A(2,3)$   
ans = -9

# Array Addressing

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- ▶ To address sub-matrices in a matrix, we use the colon (:) notation. Consider the following matrix:

- ▶  $A = [5 \ 6 \ 9; 3 \ 2 \ 7; 1 \ 4 \ 8]$

$$A = \begin{array}{ccc} 5 & 6 & 9 \\ 3 & 2 & 7 \\ 1 & 4 & 8 \end{array}$$

- ▶ The elements of the sub-matrix are in rows (2 to 3), and in columns (1 to 2), this sub-matrix is addressed such that:

- ▶  $A(2:3, 1:2)$   
ans =  $\begin{array}{cc} 3 & 2 \\ 1 & 4 \end{array}$

# Array Addressing

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▶ `>> A=[5 6 9;3 2 7;1 4 8]`

A =

5	6	9
3	2	7
1	4	8

elements from (1<sup>st</sup> and 3<sup>rd</sup> row) and (1<sup>st</sup> and 2<sup>nd</sup> column)

▶ `A([1 3],[1 2])`

ans = 5 6  
1 4

# Array Addressing

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- ▶ To address all elements from a column(s) or a row(s):

A =	5	6	9
	3	2	7
	1	4	8

- ▶ Using (:) in the  $i^{\text{th}}$  dimension selects all elements belonging to this dimension.

```
A(:,2)
ans =
     6
     2
     4
```

# Modifying array elements

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- ▶ Modifying array elements can be done by assigning new elements to sub-parts of the array.



- ▶  $A(2:3,1:2)=[5\ 8;6\ 3]$

A =

5	6	9
5	8	7
6	3	8

# Adding elements to arrays

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- ▶ Adding new elements to a matrix:
  - ▶ Assigning matrices to new positions in a matrix (at positions “outside” matrix dimension)
  - ▶ Appending two matrices
  - ▶ The added and original matrices should have the same number of rows (columns) if we are appending elements horizontally (vertically).



# Adding elements to arrays

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▶ Example:  $A = \begin{bmatrix} 5 & 6 & 9 \\ 3 & 2 & 7 \\ 1 & 4 & 8 \end{bmatrix}$

▶ Adding a column to  $A$  as a 5<sup>th</sup> column:

$A(:,5)=[3;7;2]$

$A = \begin{bmatrix} 5 & 6 & 9 & 0 & 3 \\ 3 & 2 & 7 & 0 & 7 \\ 1 & 4 & 8 & 0 & 2 \end{bmatrix}$

▶ Note that the 4<sup>th</sup> column is automatically created and set to 0, and in this horizontal appending, the number of rows of the original and added matrices are equal.

# Adding elements to arrays

---

- ▶ Adding a single element to an array is always allowed (without constraints on the size of the matrix).

$$A = \begin{matrix} 5 & 6 & 9 \\ 3 & 2 & 7 \\ 1 & 4 & 8 \end{matrix}$$

- ▶  $A(5,4)=2$

$$A = \begin{matrix} 5 & 6 & 9 & 0 \\ 3 & 2 & 7 & 0 \\ 1 & 4 & 8 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 2 \end{matrix}$$

- ▶ New elements are created accordingly to satisfy the new matrix dimension (and are set to 0).

# Adding elements to arrays

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- ▶ Another method of appending elements of two arrays is by assigning a new array whose elements are arrays and not scalars.

- ▶  $A=[1\ 2;5\ 6]$

$A = \begin{matrix} 1 & 2 \\ 5 & 6 \end{matrix}$

- ▶  $B=[7;8]$

$B = \begin{matrix} 7 \\ 8 \end{matrix}$

- ▶  $C=[A\ B]$

$C = \begin{matrix} 1 & 2 & 7 \\ 5 & 6 & 8 \end{matrix}$

# Deleting elements from arrays

---

- ▶ Deleting columns or rows from a matrix can be done by assigning the **null matrix [ ]** to a sub-part of the matrix.

- ▶  $A = \begin{matrix} 5 & 6 & 9 \\ 3 & 2 & 7 \\ 1 & 4 & 8 \end{matrix}$

- ▶  $A(:,2) = []$   
 $A = \begin{matrix} 5 & 9 \\ 3 & 7 \\ 1 & 8 \end{matrix}$

# Array Functions

Function	Description	Example
<code>reshape(X,M,N)</code>	Returns the M-by-N matrix whose elements are taken column wise from X.	<pre>X=[1 2;3 4]; Y=reshape(X,1,4) Y = 1  3  2  4</pre>
<code>diag(v)</code>	Returns a matrix and puts the elements of v in the main diagonal	<pre>v=[1 2 3]; A=diag(v) A =  1  0  0      0  2  0      0  0  3</pre>
<code>reshape(X,M,N)</code>	Returns the M-by-N matrix whose elements are taken column wise from X.	<pre>X=[1 2;3 4]; Y=reshape(X,1,4) Y = 1  3  2  4</pre>
<code>[M,N]=size(X)</code>	for matrix X, returns the number of rows and columns in X as separate output variables.	<pre>X=[1 2 3;7 5 9]; [M N]=size(X) M=2 &amp; N=3</pre>

# Simple plot with MATLAB

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- ▶ Use “**plot**” command:
  - ▶ `plot(t, x)`
  - ▶ Plots the vector “**x**” against the vector “**t**”
- ▶ **Example:**  
Plot the function  $x=2\exp(-2t)$  over the range  $[0;2]$ 
  - ▶ `t=0:0.1:2;`
  - ▶ `x=2*exp(-2*t);`
  - ▶ `plot(t,x)`
  - ▶ `grid`

# Simple plot with MATLAB

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